

# Phase Noise under Vibration Theory and Test Results

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# Content



## ✘ Theoretical Background

- ✘ Sensitivity to forces and acceleration
- ✘ Sensitivity to vibrations

## ✘ Experimental Results

- ✘ AXIOM75-16-60 MHz with AT-cut (HC-43/U)
- ✘ AXIOM75-16A-60 MHz with SC-cut (HC-35/U)
- ✘ AXIOM35-14A-100 MHz with SC-cut (HC-43/U)
- ✘ 100 MHz with SC-cut (HC-43/U) other supplier

# Content



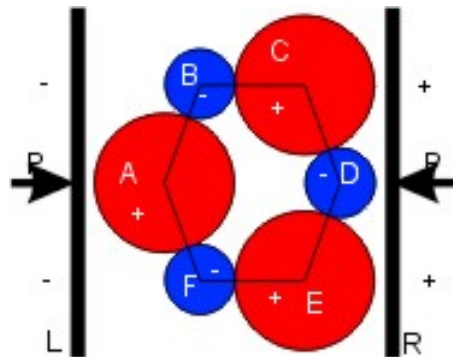
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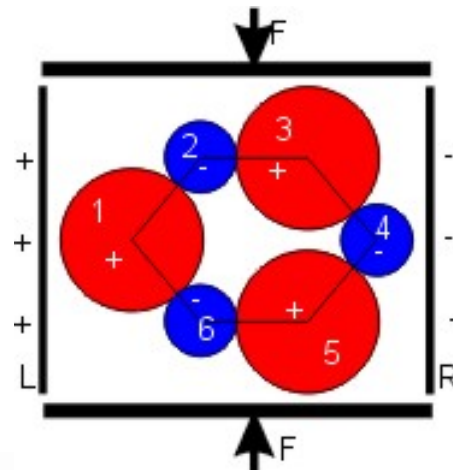
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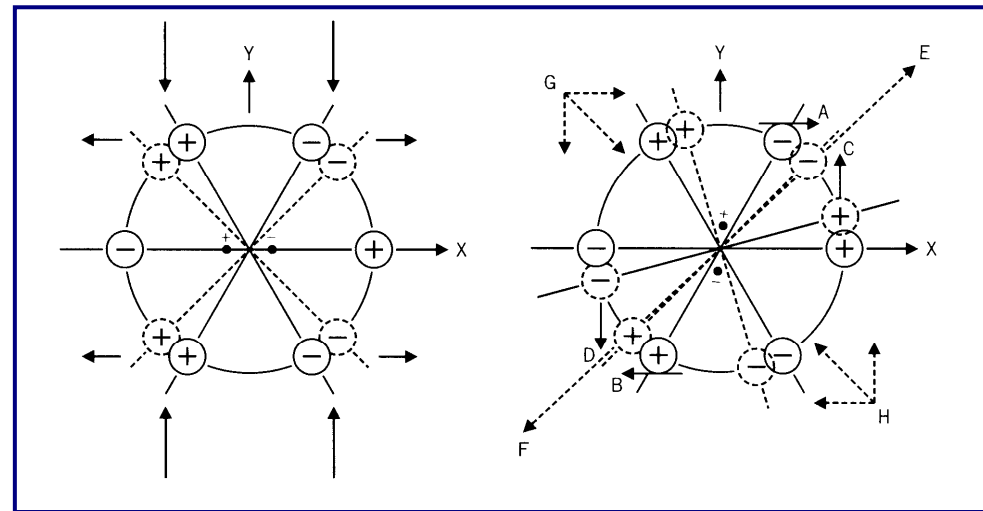
# Piezo-electrical Effect



Longitudinal PE



Transversal PE



Mechanical force (pressure) creates electrical charge (voltage) and vice versa

# Most popular cuts

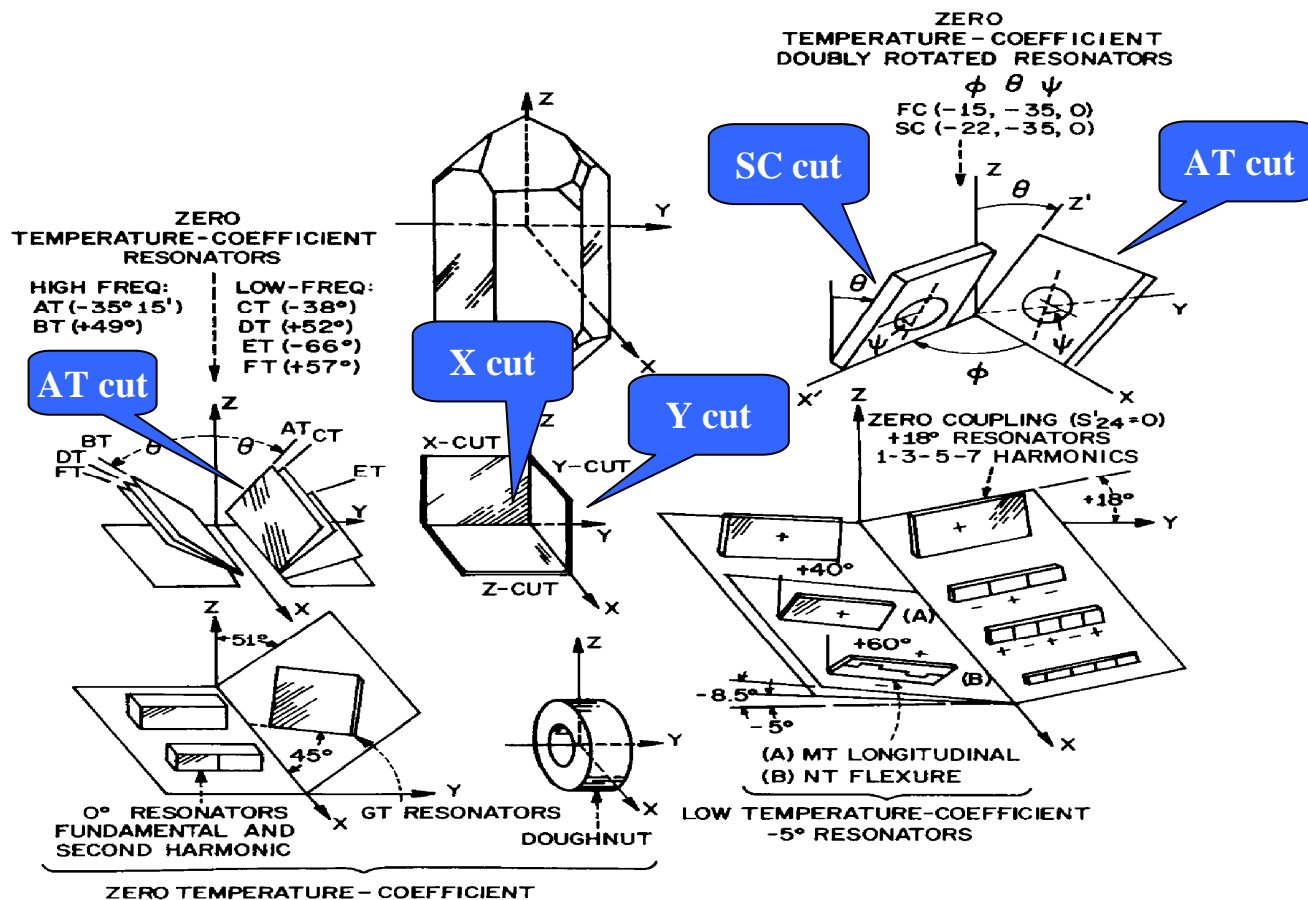
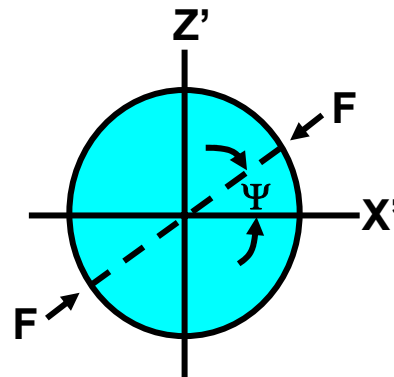


FIG. 2.2-6 Principal cuts of right-hand alpha quartz.

# Influence of lateral forces

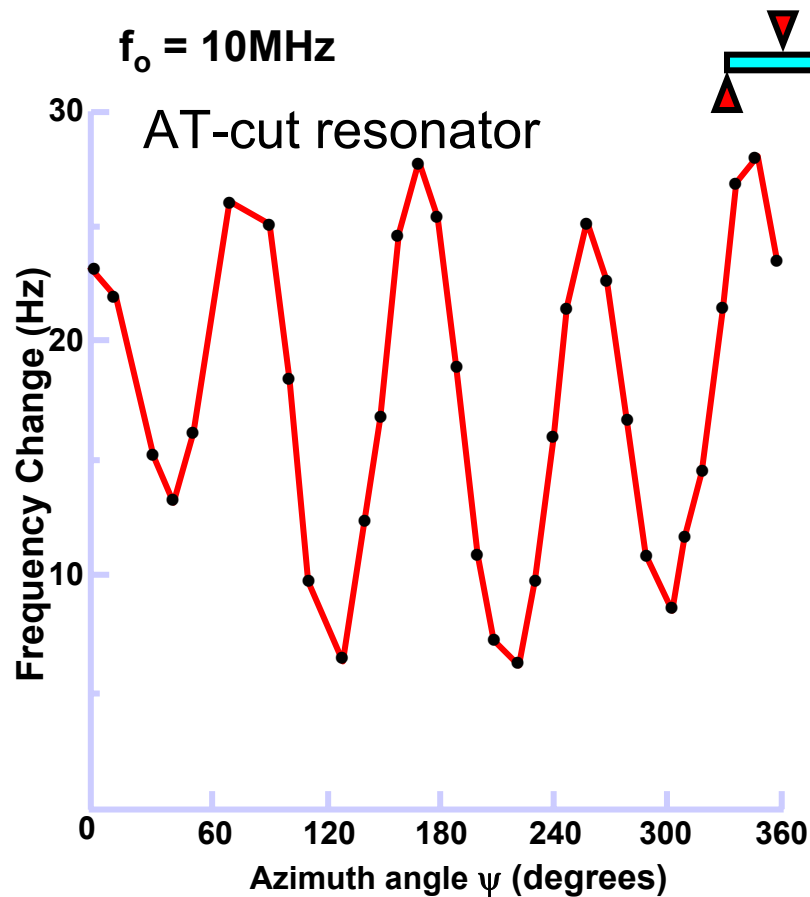


Example:

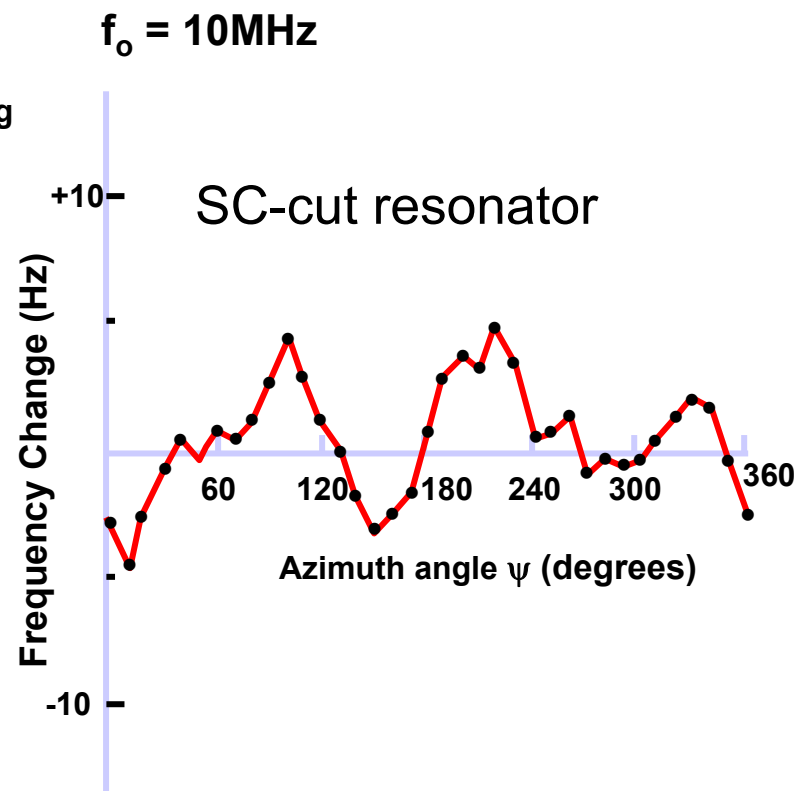
Resonator 5 MHz 3rd overtone, 14 mm diameter

$$\left(\frac{\Delta f}{f}\right)_{\text{Max}} = \begin{cases} 3 \text{ ppm/N} & \text{for AT-cut resonator} \\ 1.7 \text{ ppm/N} & \text{for SC-cut resonator} \end{cases}$$

# Influence of bending forces

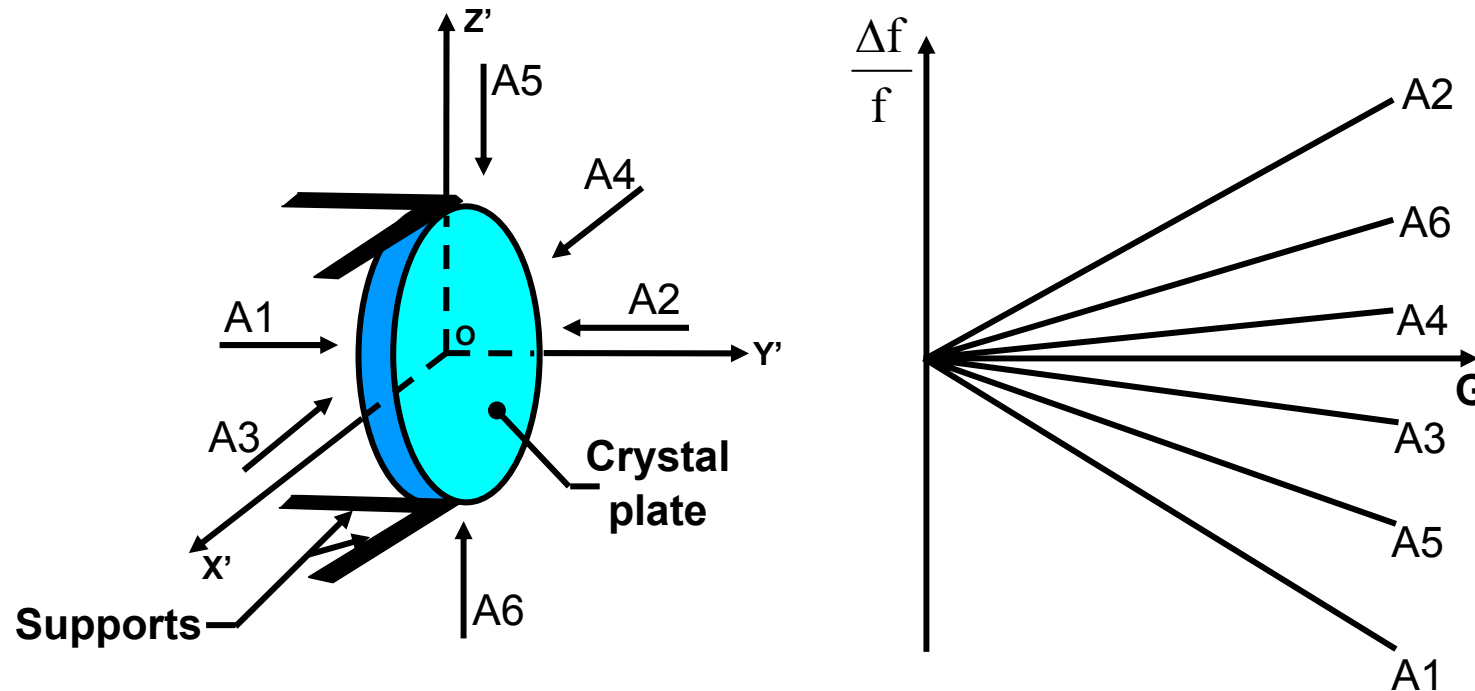


Frequency change for symmetrical bending, AT-cut crystal.



Frequency change for symmetrical bending, SC-cut crystal.

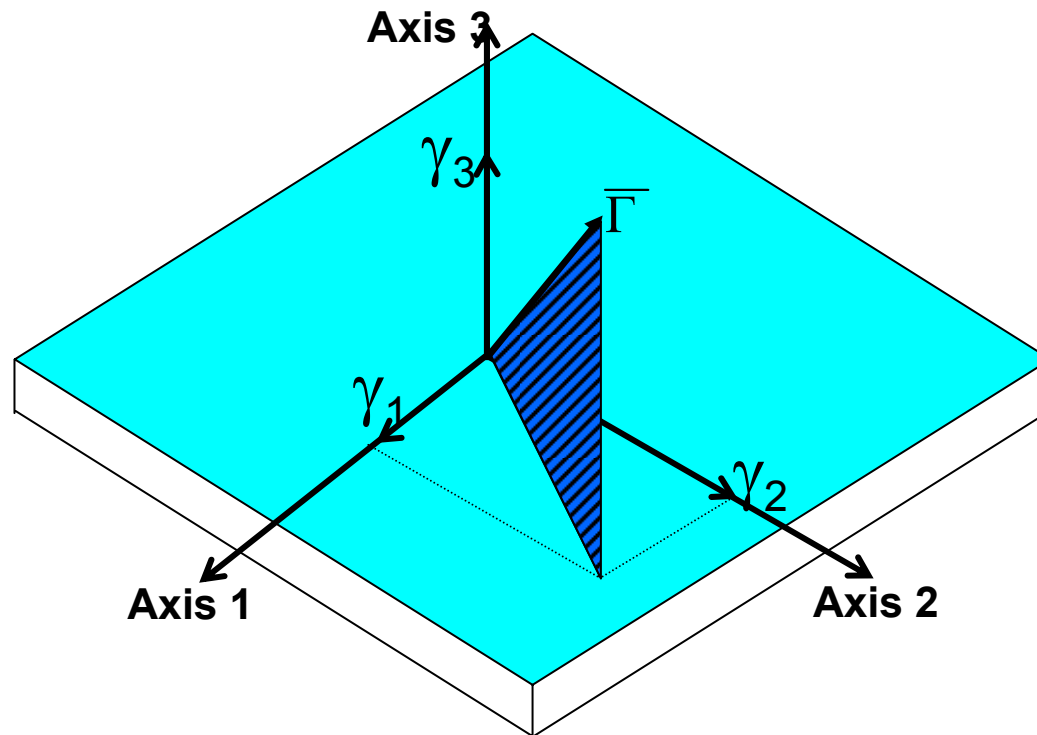
# Frequency change with acceleration



Strains due to acceleration cause frequency changes.  
Under vibration, the time varying strains cause  
time dependent frequency changes, i.e. frequency modulation



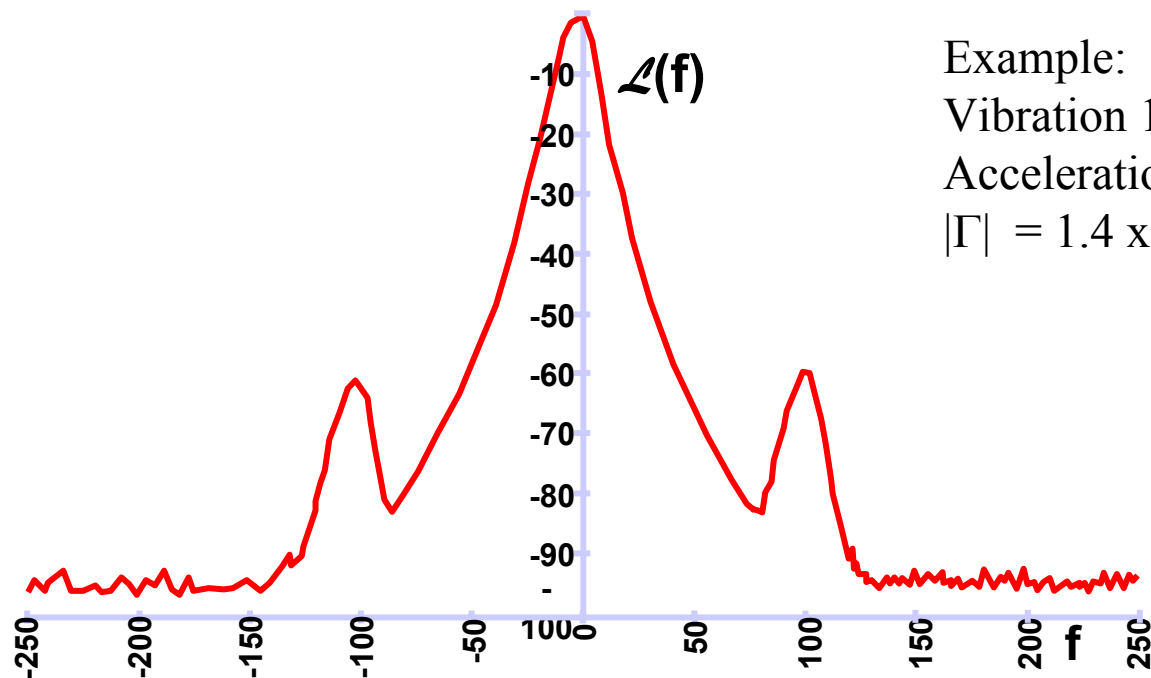
# Acceleration Sensitivity Vector



$$\bar{\Gamma} = \gamma_1 \hat{i} + \gamma_2 \hat{j} + \gamma_3 \hat{k}$$

$$\Gamma = \sqrt{\gamma_1^2 + \gamma_2^2 + \gamma_3^2}$$

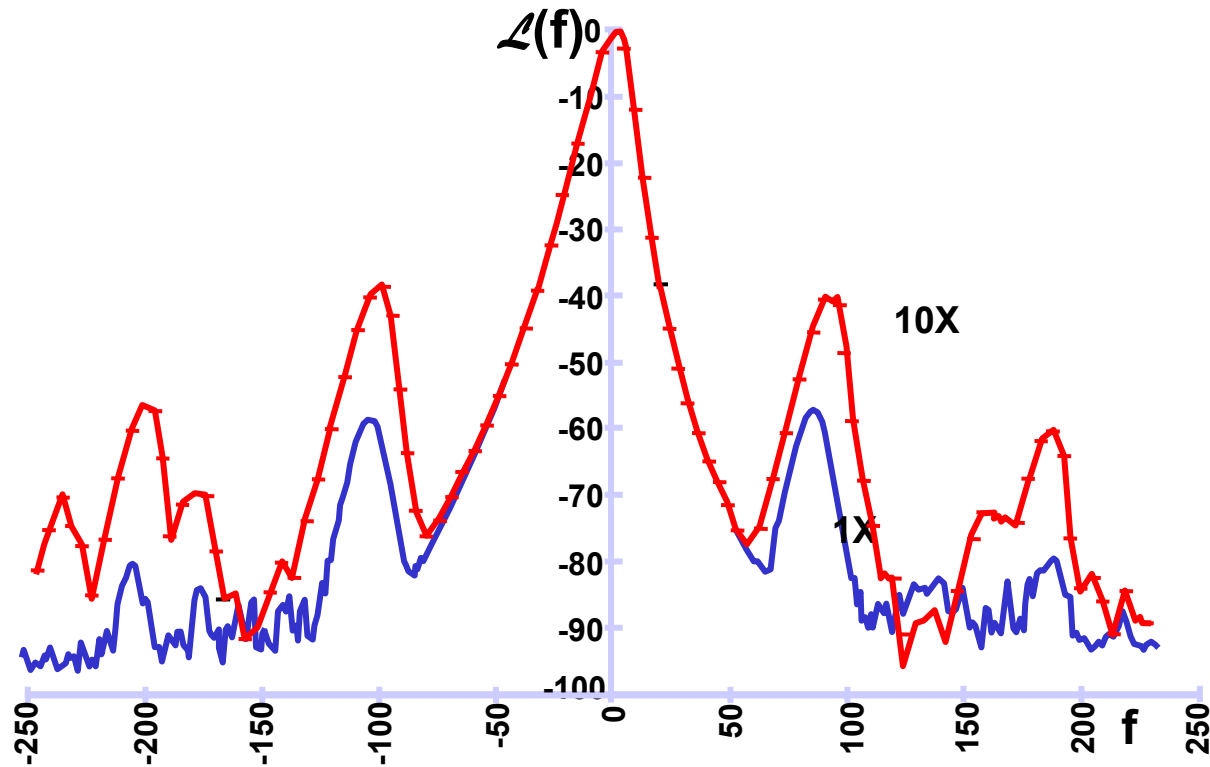
# Sine Vibration Induced Sidebands



Example:  
Vibration 10 G @ 100 Hz  
Acceleration sensitivity vector  
 $|\Gamma| = 1.4 \times 10^{-9} / \text{G}$

Sinusoidal vibration with vibration frequency  $f_v$   
produces spectral lines at  $\pm f_v$  from the carrier

# Frequency Multiplication



Each frequency multiplication by 10 increases the sidebands by 20 dB

$$\Delta a = 20 \cdot \log(N)$$

# Sine Vibration Induced Sidebands



Sinusoidal vibration produces spectral lines at  $\pm f_v$  from the carrier, where  $f_v$  is the vibration frequency.

$$\mathcal{L}(f_v) = 20 \log \left( \frac{\bar{\Gamma} \cdot \bar{A} f_0}{2f_v} \right)$$

e.g., if  $|\bar{\Gamma}| = 1 \times 10^{-9}/G$  and  $f_0 = 10$  MHz, then even if the oscillator is completely **noise free at rest**, the spectral lines due solely to a sine vibration level of 1G are:

Vibr. freq., $f_v$ [Hz]	$\mathcal{L}(f_v)$ [dBc]
1	-46
10	-66
100	-86
1,000	-106
10,000	-126

# Random Vibration Induced Phase Noise



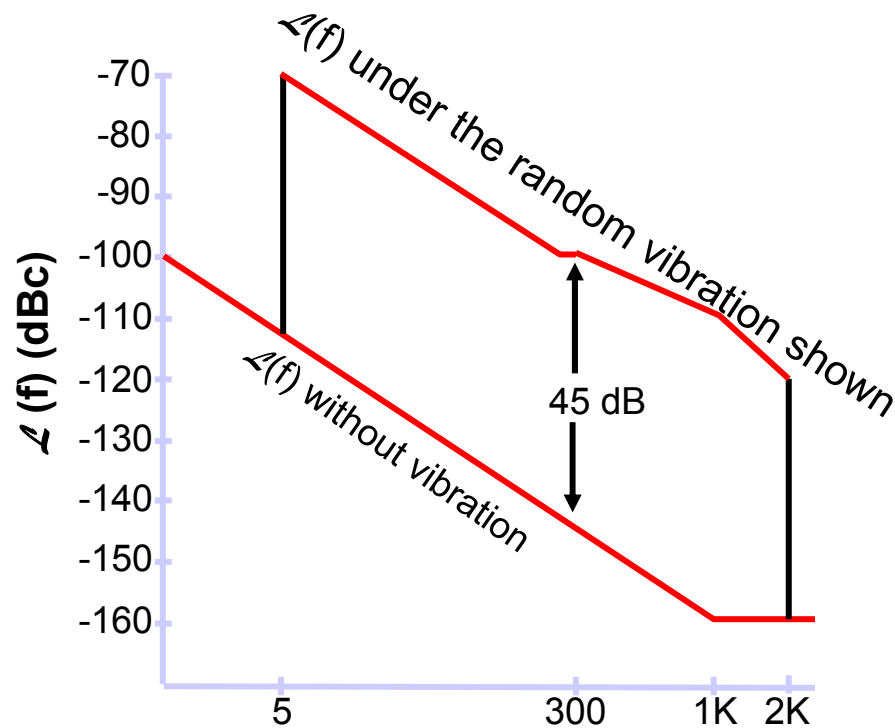
Random vibration's contribution to phase noise is given by:

$$\mathcal{L}(f) = 20 \log \left( \frac{\bar{\Gamma} \cdot \bar{A}f_0}{2f} \right), \quad \text{where } |\bar{A}| = [(2)(\text{PSD})]^{1/2}$$

e.g., if  $|\Gamma| = 1 \times 10^{-9}/G$  and  $f_0 = 10$  MHz, then even if the oscillator is completely **noise free at rest**, the phase “noise” i.e., the spectral lines, due solely to a vibration of power spectral density,  $\text{PSD} = 0.1 \text{ g}^2/\text{Hz}$  will be:

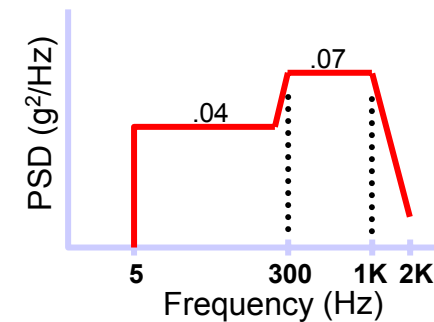
Offset freq. $f$ [Hz]	$\mathcal{L}'(f)$ [dBc/Hz]
1	-53
10	-73
100	-93
1,000	-113
10,000	-133

# Random Vibration Induced Phase Noise

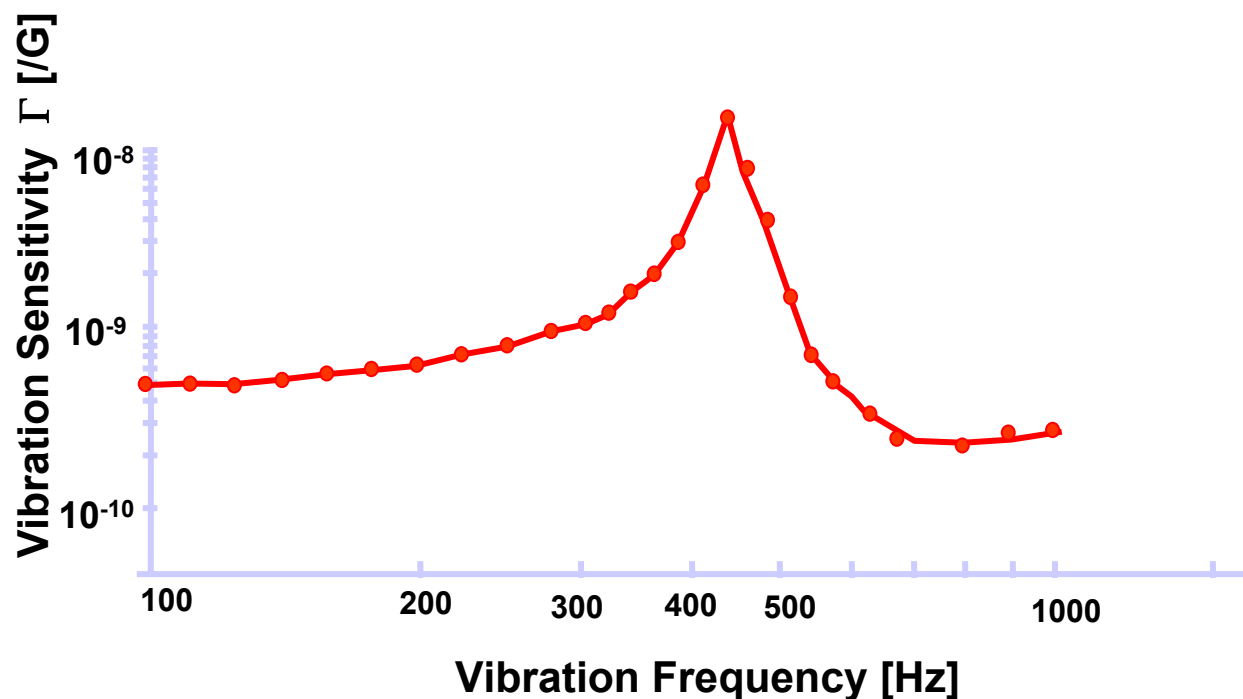


Random Vibration for a Crystal with Vibration Sensitivity of  $|\Gamma| = 1 \times 10^{-9}/G$   
Osc frequency  $f_0 = 10$  MHz

Vibration profile (aircraft):



# Acceleration Sensitivity with Resonances



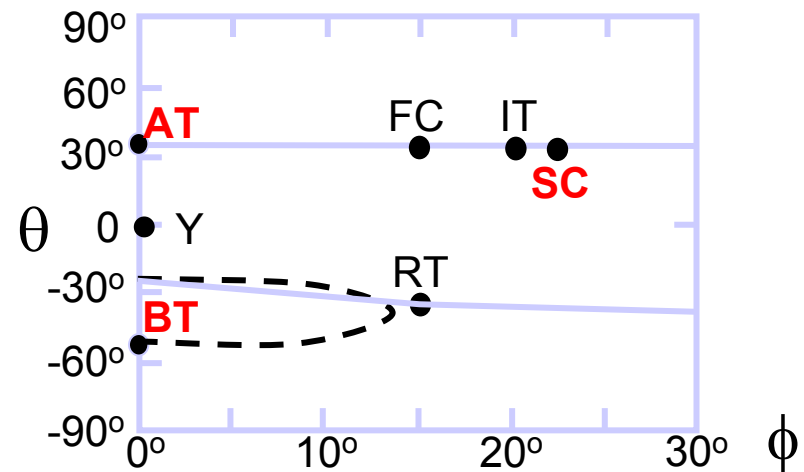
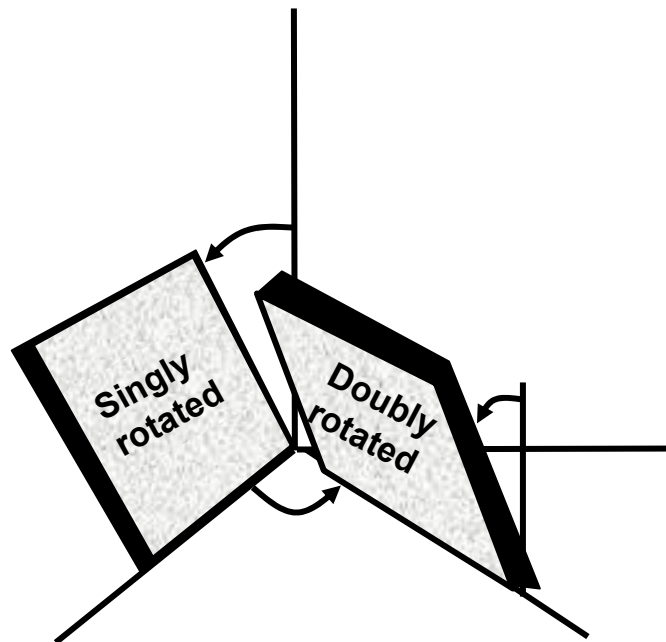
In an ideal oscillator,  $\Gamma(fv)$  would be constant, but real oscillators exhibit resonances which increase the  $\Gamma$  in the relevant frequency band

# Factors determining Acceleration Sensitivity

- ✘ Crystal cut
- ✘ Crystal holder
- ✘ Mounting structure
- ✘ Crystal design
  - ✘ symmetrical shape of crystal blank (contour), electrodes and mounting structure
- ✘ G-Sensitivity of other components



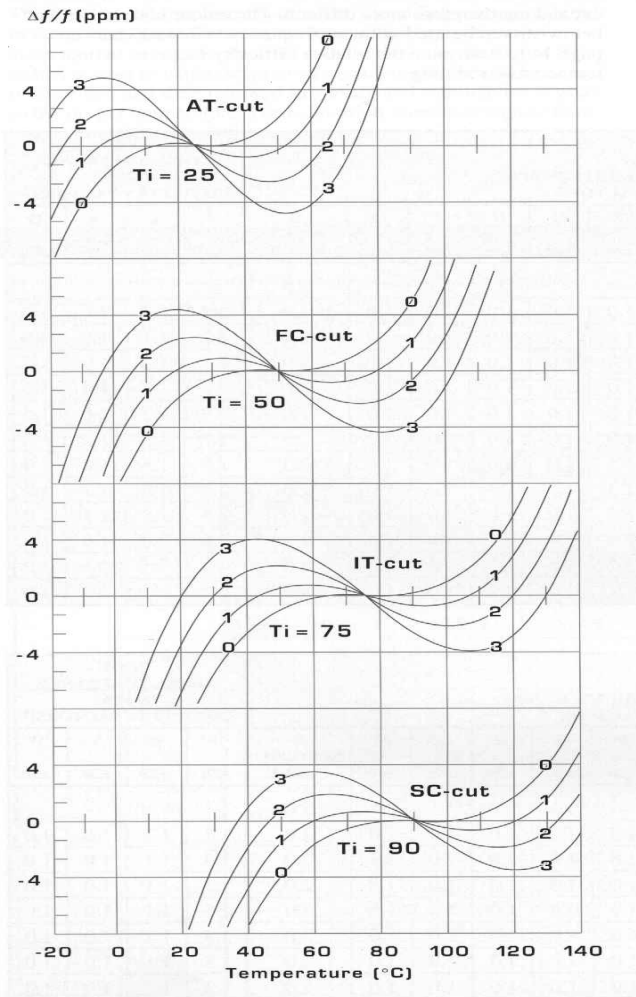
# Cuts with zero TC (Thickness shear)



$\Theta \approx 35^\circ$ : AT cut: TC = 0 ppm/K at  $\approx 25^\circ\text{C}$   
 SC cut\*: TC = 0 ppm/K bei  $\approx 95^\circ\text{C}$

\*SC = Stress Compensated

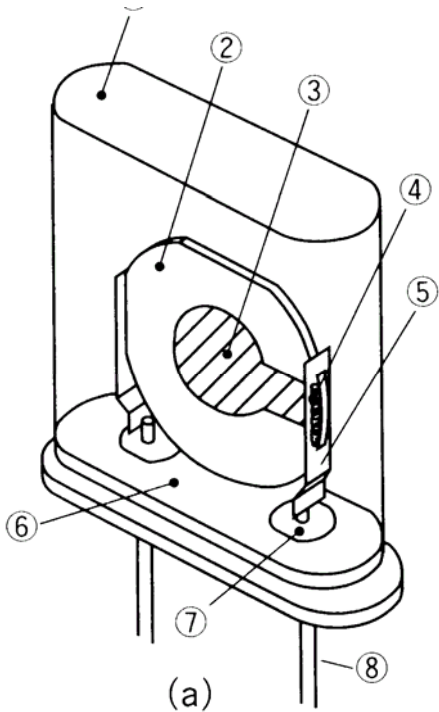
# $f(T)$ for doubly rotated cuts



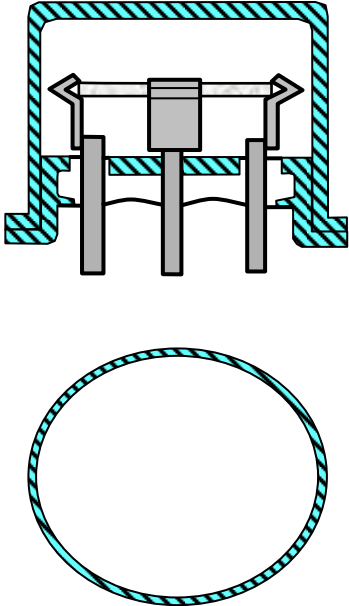
The inflection temperature moves up with increasing 2nd rotation angle  $\Phi$ .

For  $\Phi \approx 22^\circ$  ( $T_{inv} \approx 95^\circ\text{C}$ ), the so-called SC cut („Stress Compensated) the impact of mechanical stresses on the Resonance frequency compensate

# Comparison of Crystal packages



**Two-point Mount Package**  
e.g. HC-43/U or HC-45/U

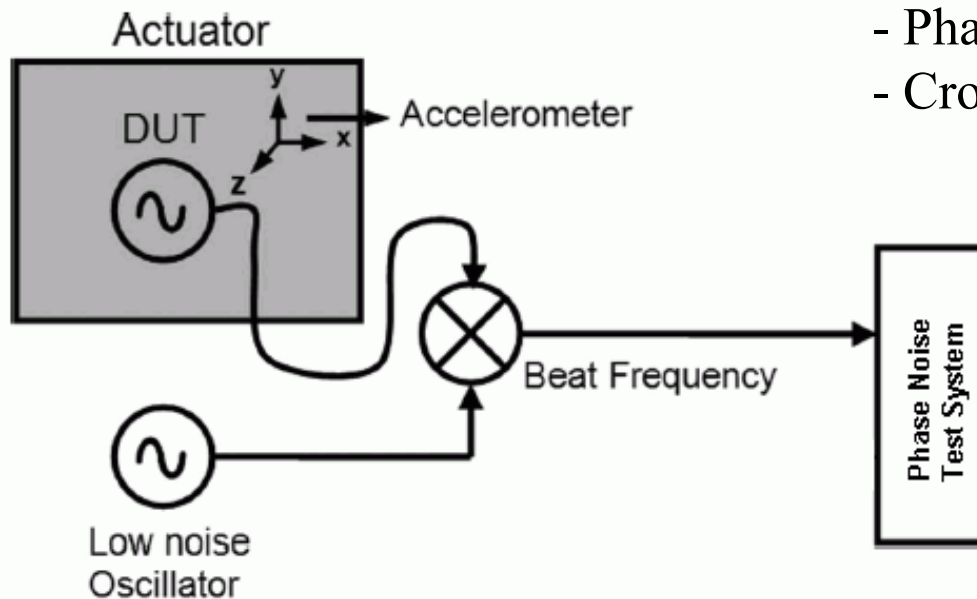


**Three- and Four-point Mount Package**  
e.g. HC-35/U or HC-37/U

# Testing of Vibration Sensitivity



## ✘ Test Setup



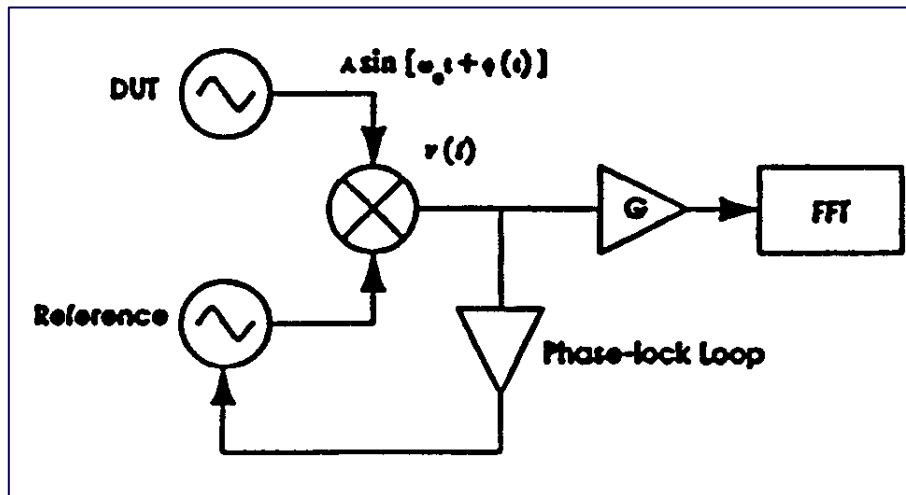
PN Test Systems:

- Phase Quadrature Method
- Cross Correlation

# Phase Noise Test



## Phase Quadrature Method



$$\Phi_{\text{det}} = K \cdot (\Phi(t) - \Phi_{\text{ref}}(t))$$

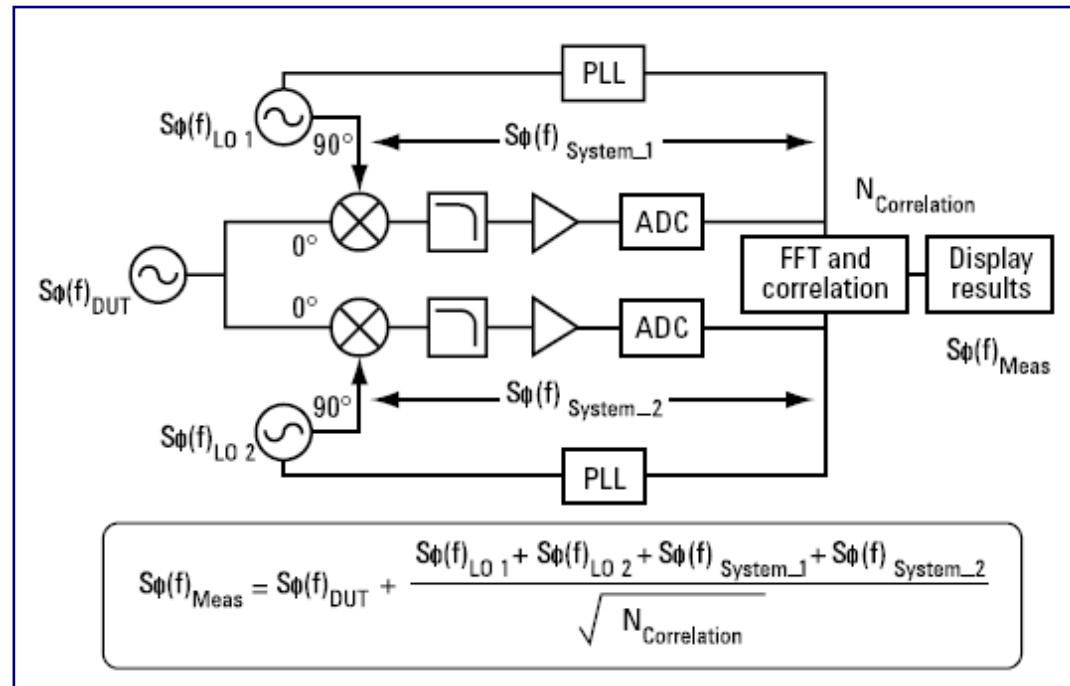
The signal under test and a signal of same frequency from a reference oscillator are combined in a phase detector. The frequency of oscillator #2 is locked to oscillator #1 by a PLL. The DC output signal of the phase detector is proportional to the phase difference of the two signals. All noise spectral components, which are „faster“ than the loop filter will be measured by the spectrum analyzer or FFT.

If the reference oscillator has very low phase noise, the measured noise is dominated by the noise of the oscillator under test.

If both oscillators have the same noise, the noise of one oscillator is -3 dB lower than the noise measured with the spectrum analyzer.

Example: Aeroflex PN9000

# Phase Noise Test



## Cross Correlation Method

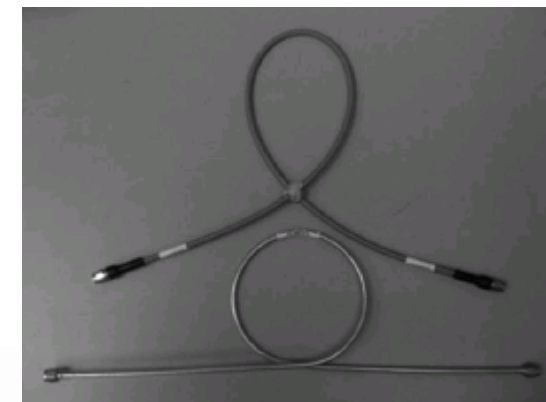
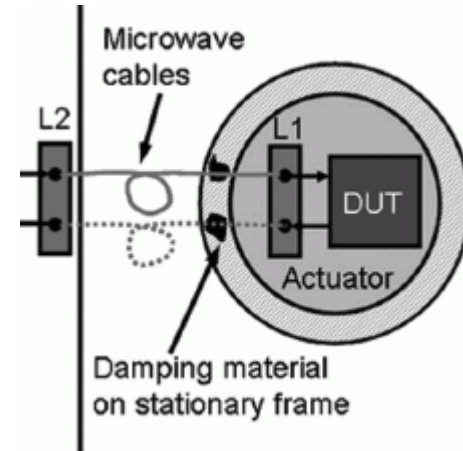
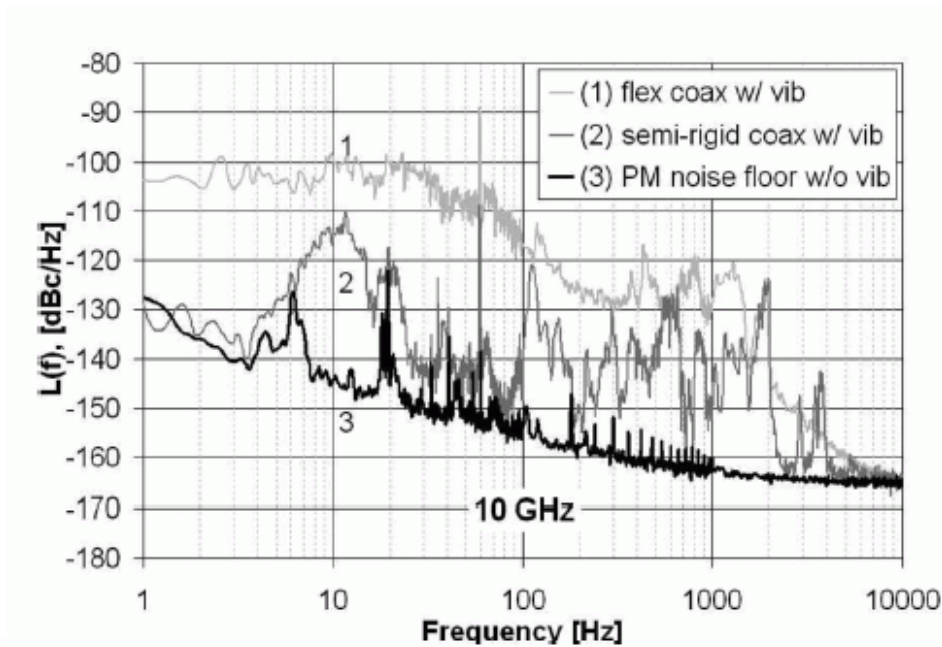
© Agilent

The signal is fed into two phase detectors and both channels are mixed with an internal low-noise reference signal. Both channels are locked to the test signal through a PLL. The noise content of the identical channels is evaluated by mathematical cross-correlation technique. Examples: Agilent Signal Source Analyzer E5052B, Rohde & Schwarz FSUP

# Testing of Vibration Sensitivity



## Cables and mounting



# Content



## ✘ Theoretical Background

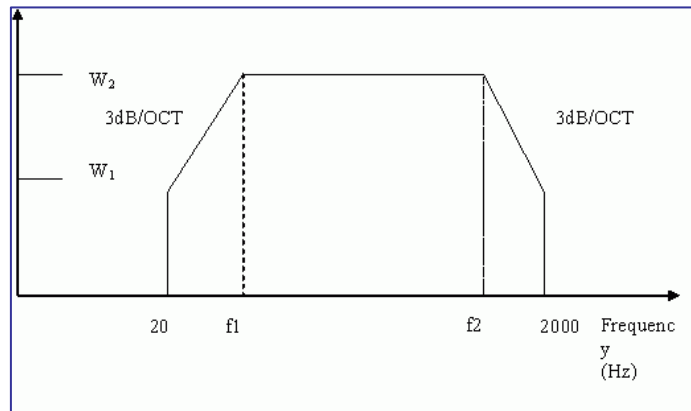
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- ✘ 60 MHz with SC-cut (HC-43/U) other vendor

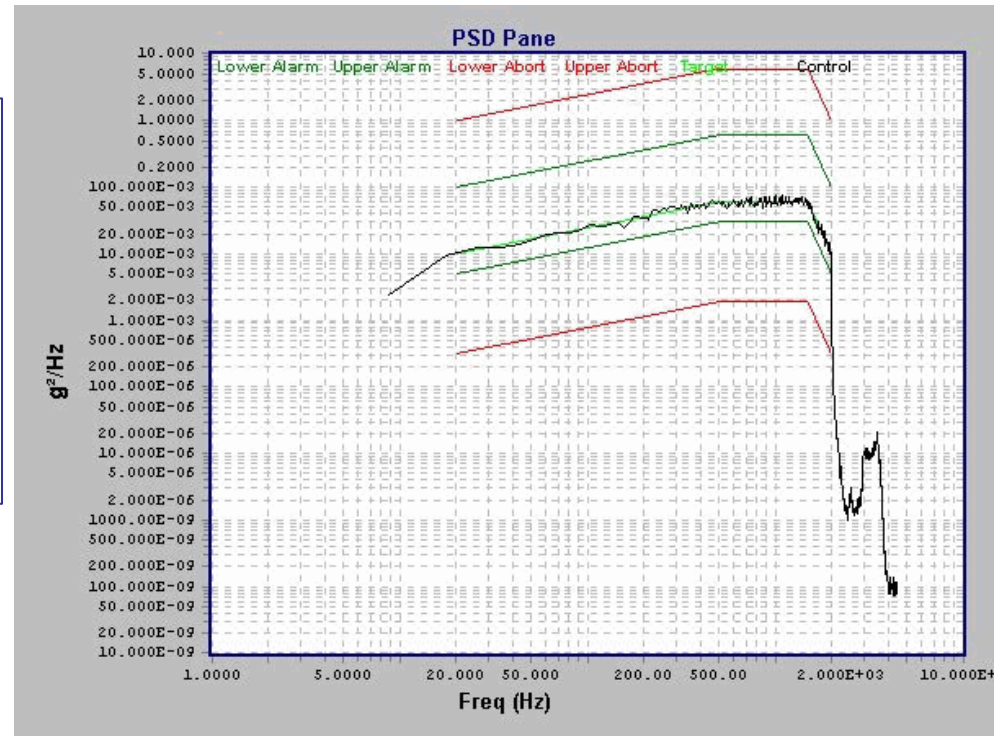


# Vibration Spectrum



$W_1=0.01g^2/Hz$ ,  $W_2=0.06g^2/Hz$

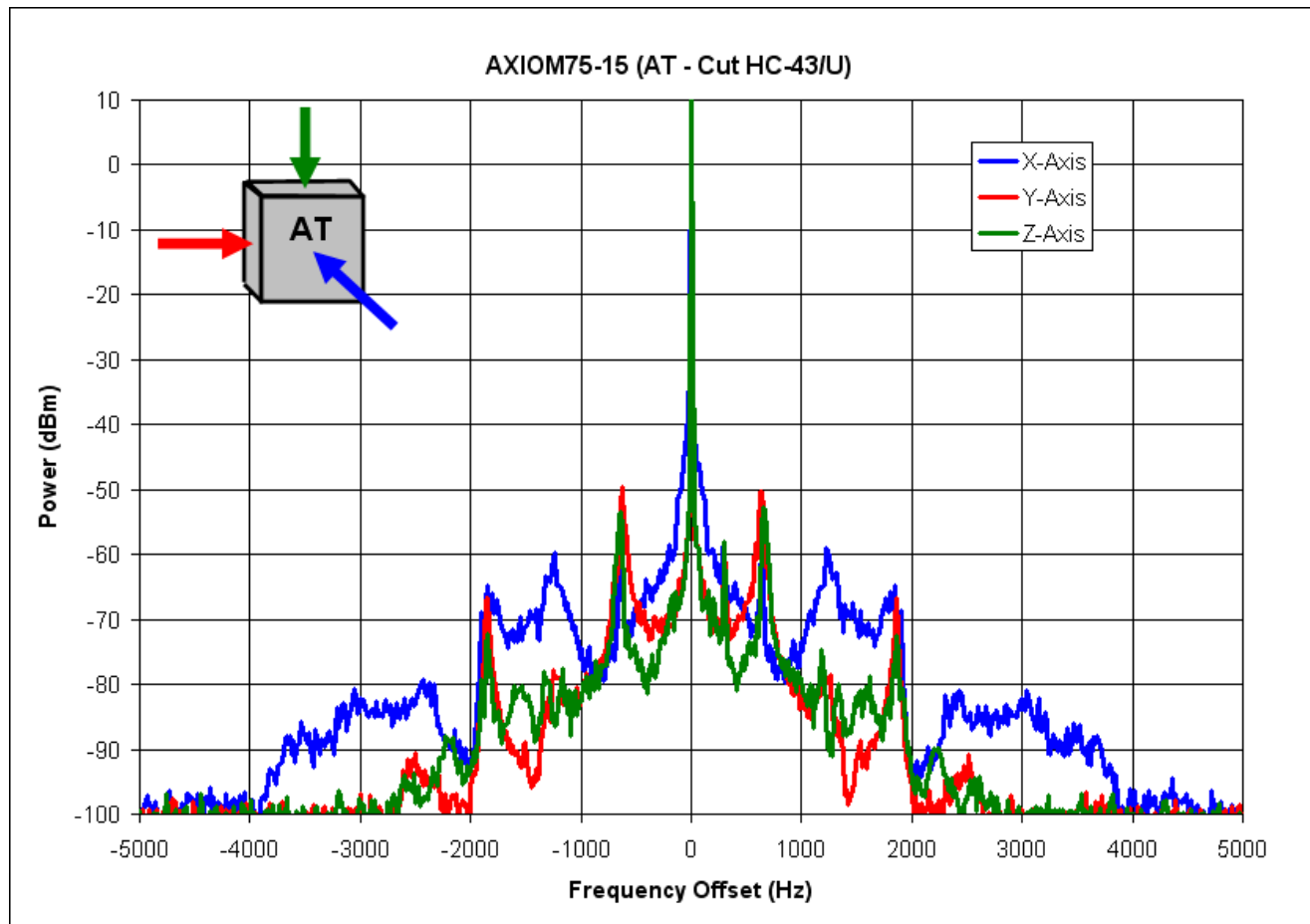
$f_1=500Hz$ ,  $f_2=1500Hz$



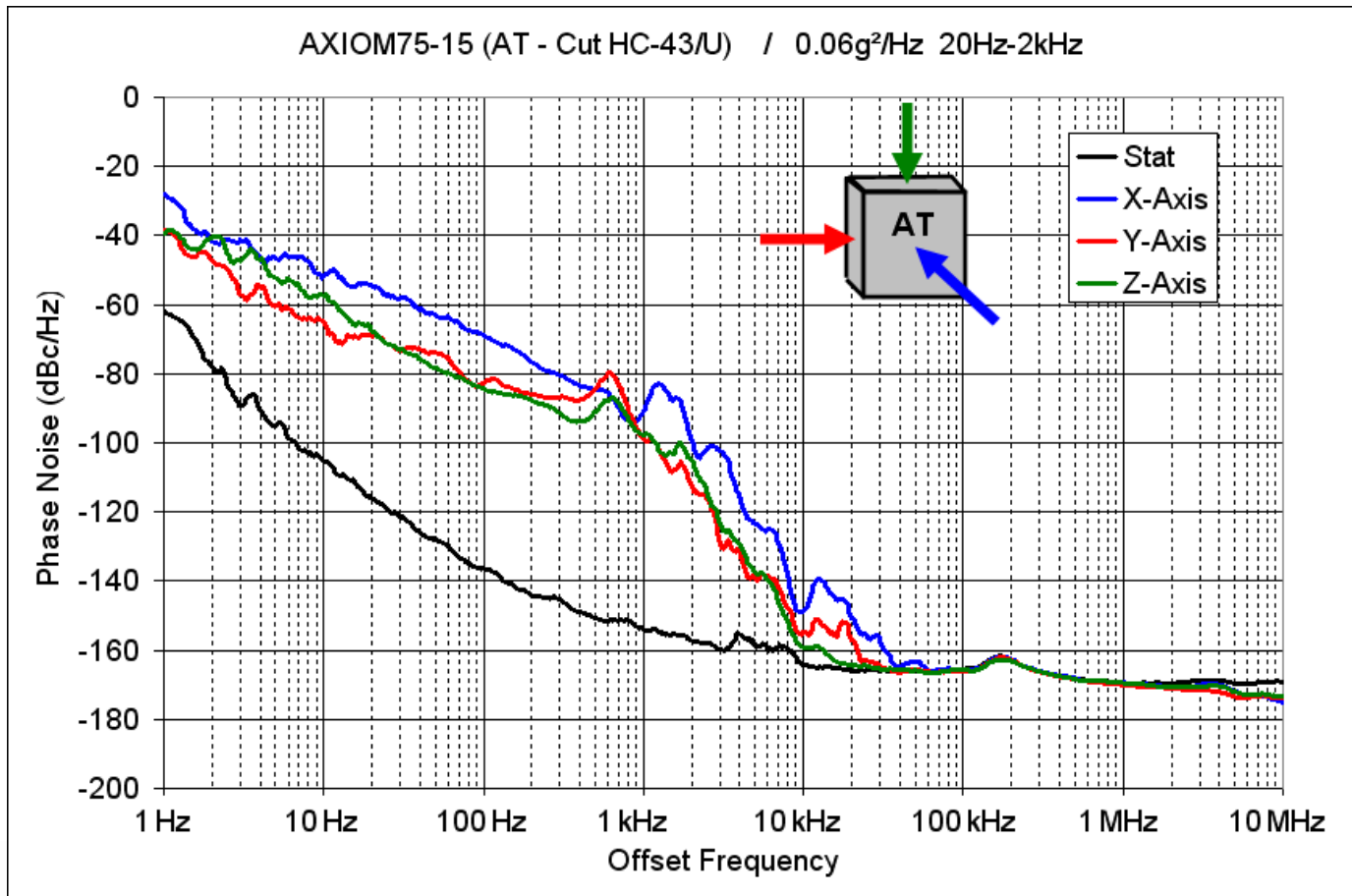
Customer spec

Tested profile

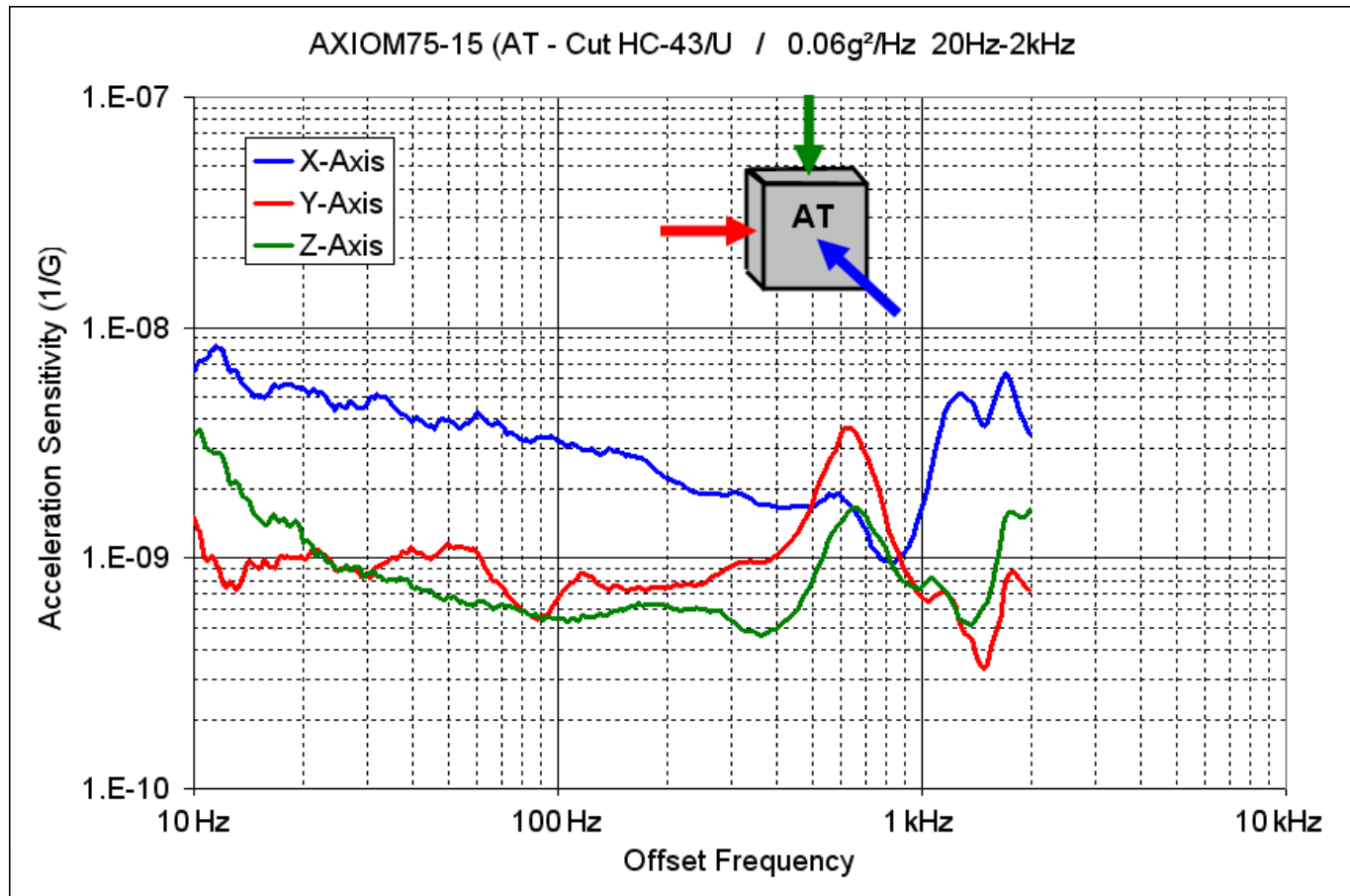
# AXIOM75-16-60 MHz AT-cut (HC-43/U) Output Spectrum



# AXIOM75-16-60 MHz AT-cut (HC-43/U) Phase Noise



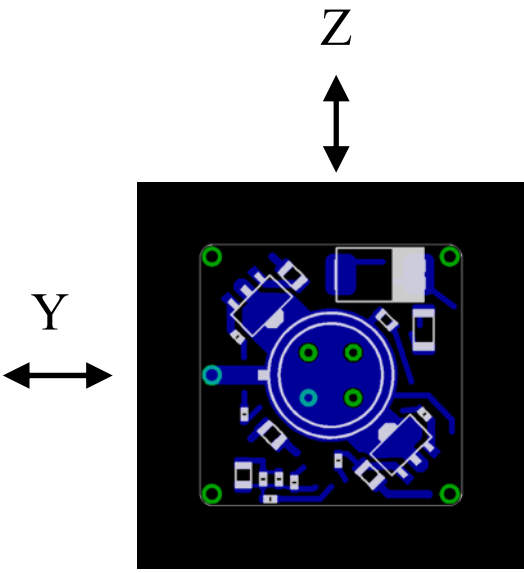
# AXIOM75-16-60 MHz AT-cut (HC-43/U) G - Sensitivity



# AXIOM75-16A-60 MHz SC-cut (HC-35/U)



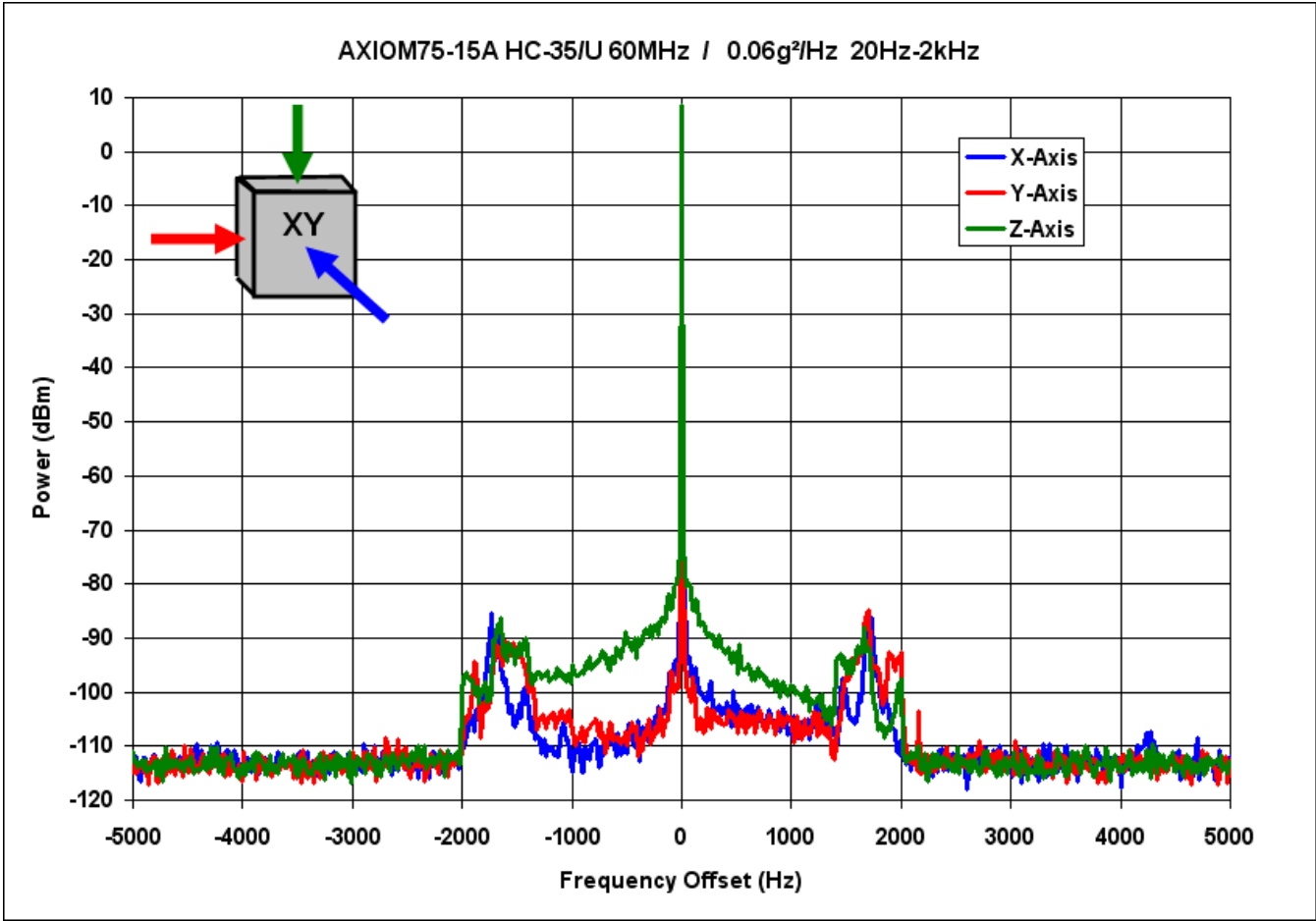
## Test fixture



Orientation

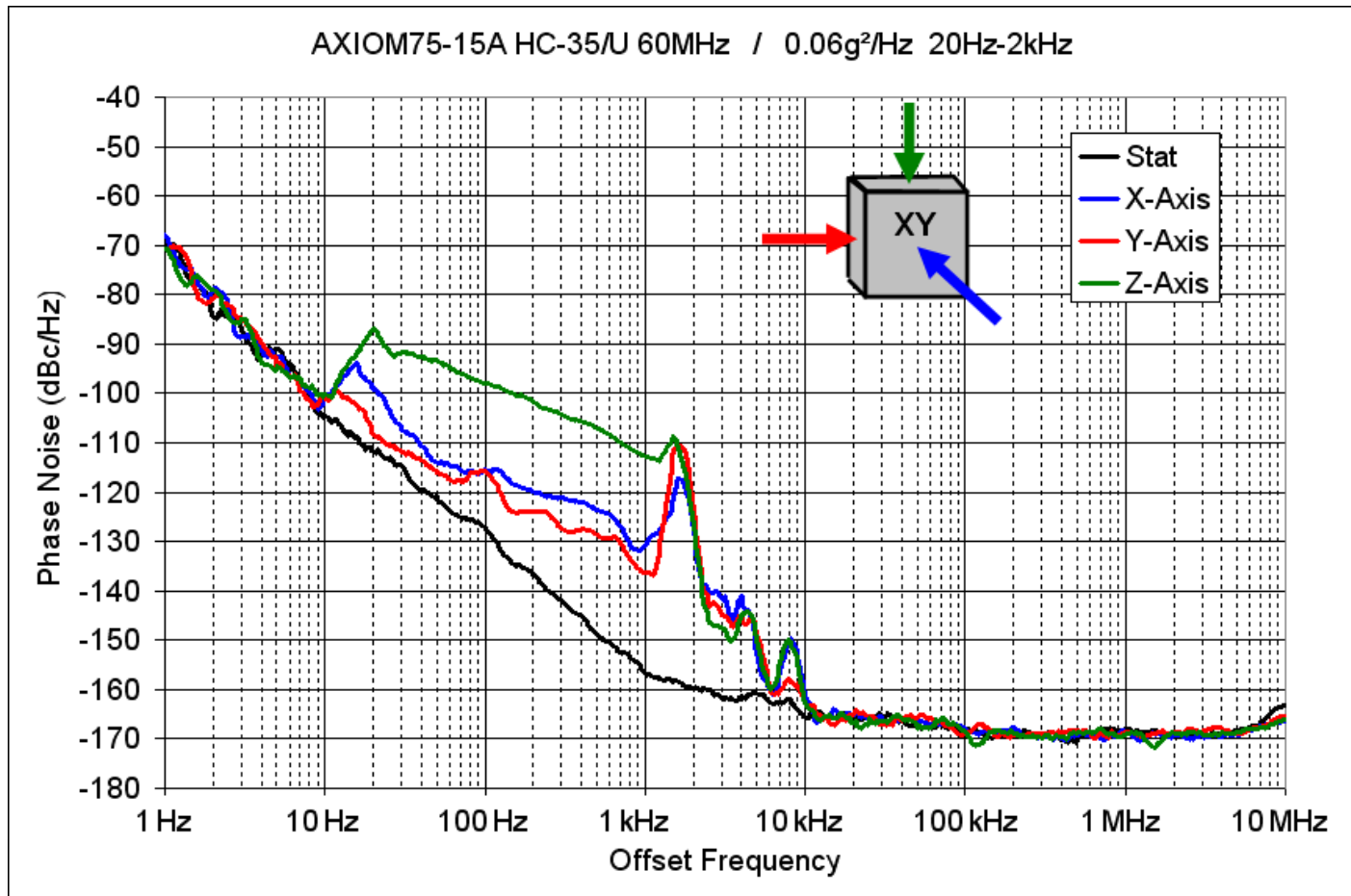


# AXIOM75-16A-60 MHz SC-cut (HC-35/U) Output Spectrum



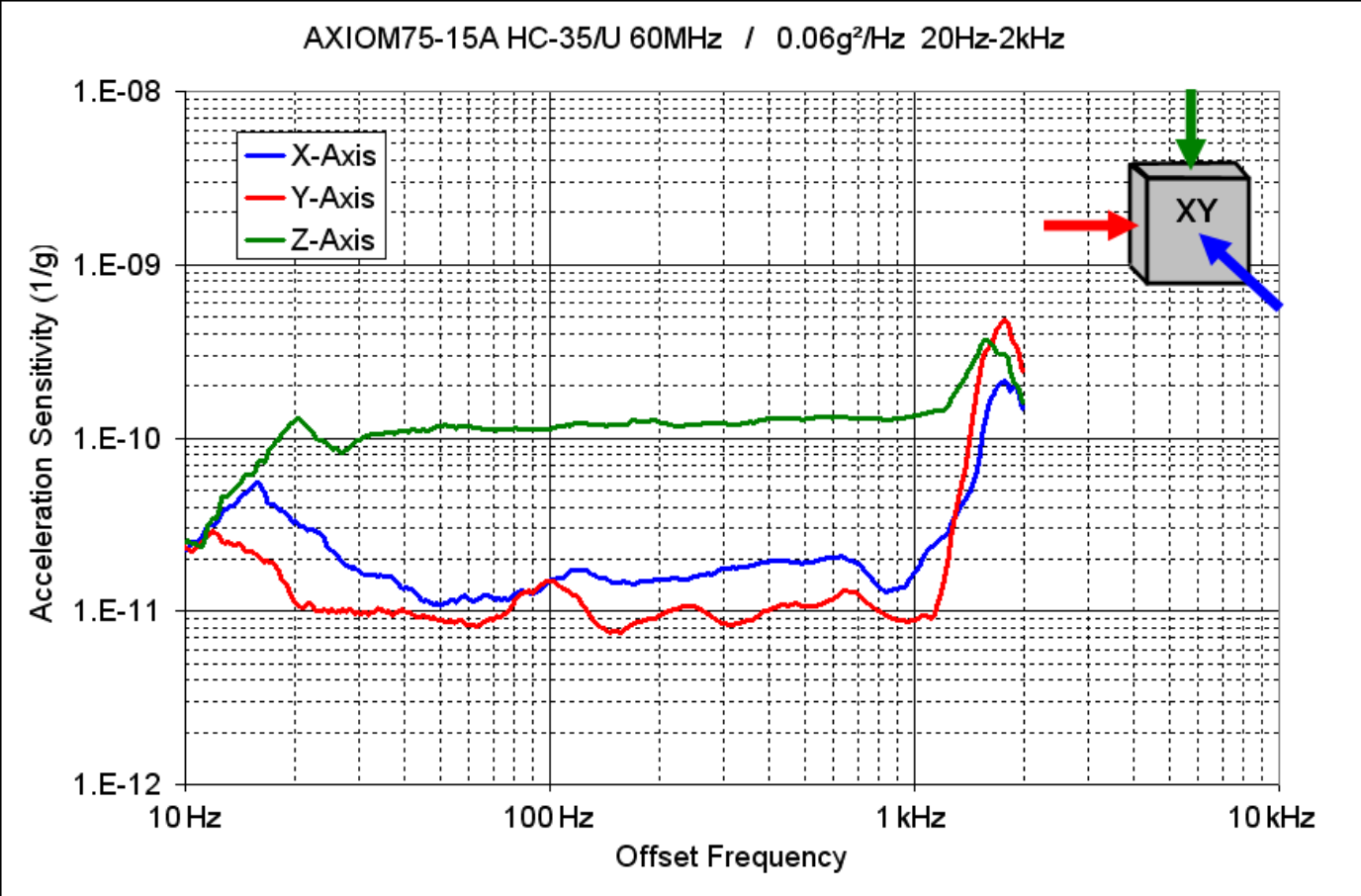
# AXIOM75-16A-60 MHz SC-cut (HC-35/U)

## Phase Noise



# AXIOM75-16A-60 MHz SC-cut (HC-35/U)

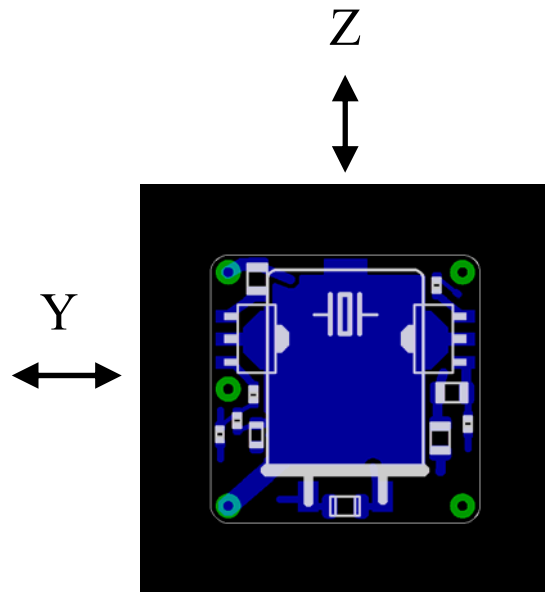
## G - Sensitivity





# AXIOM35-14A-100 MHz SC-cut (HC-43/U)

## Test fixture

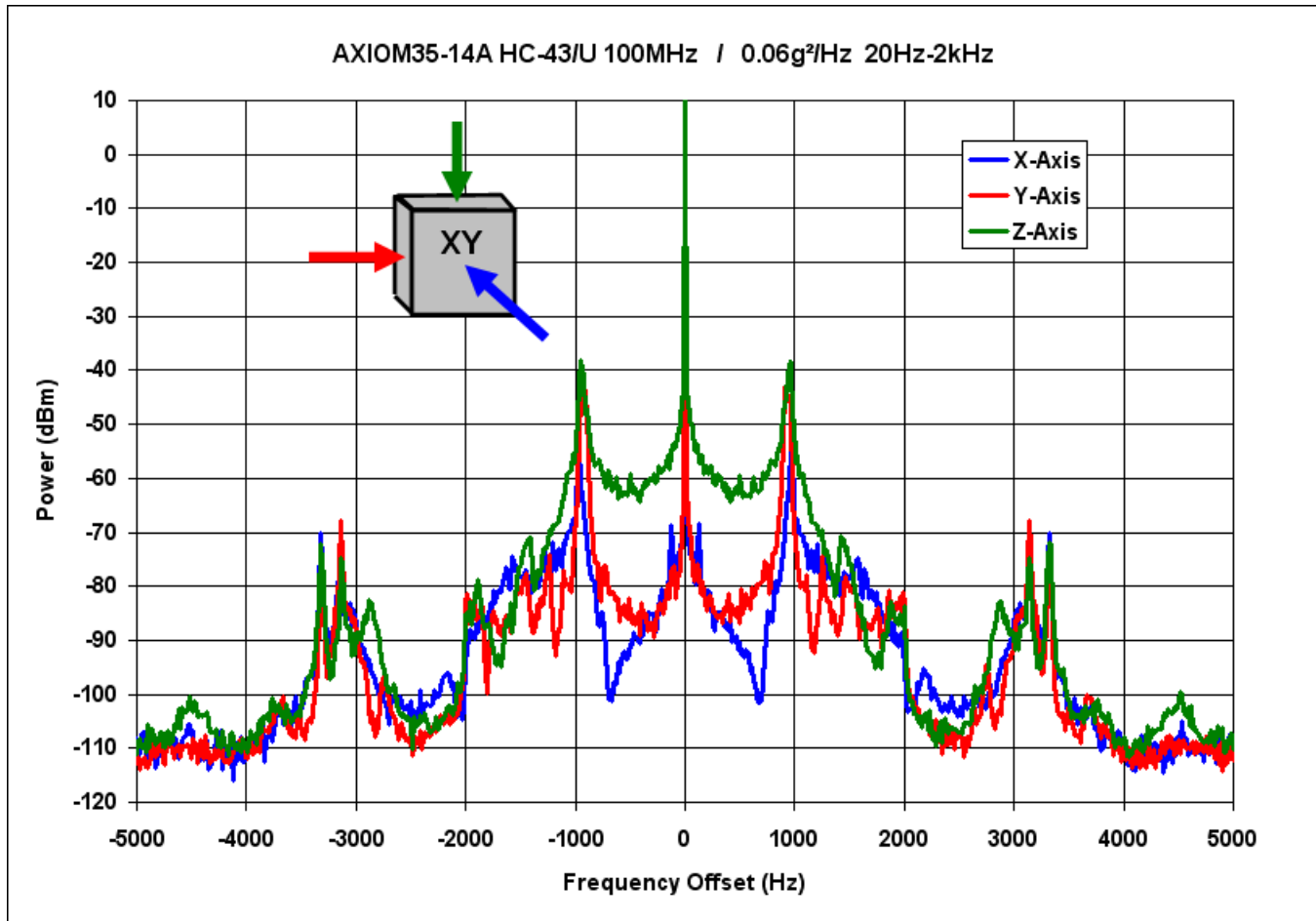


Orientation



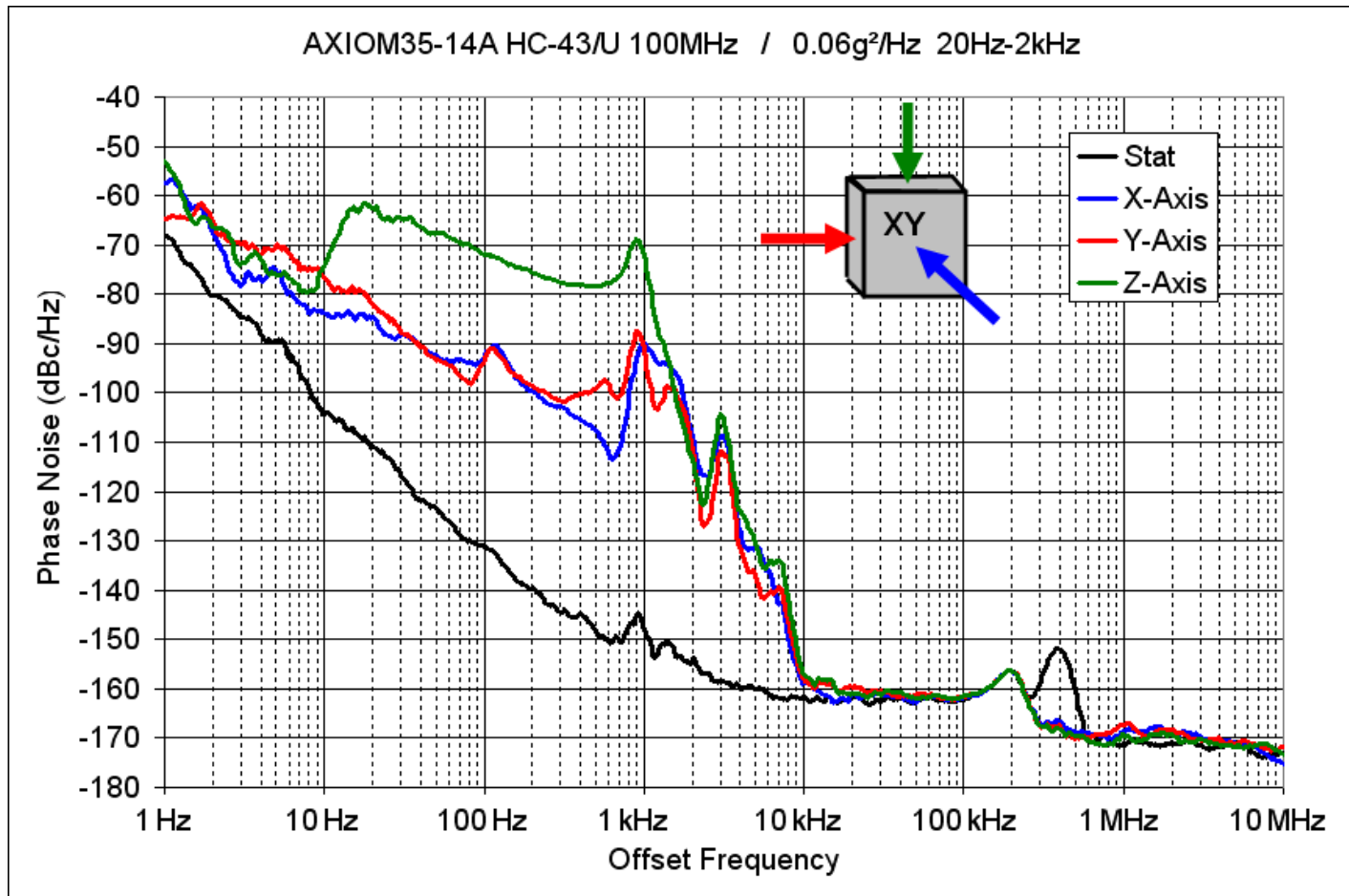
# AXIOM35-14A-100 MHz SC-cut (HC-43/U)

## Output Spectrum



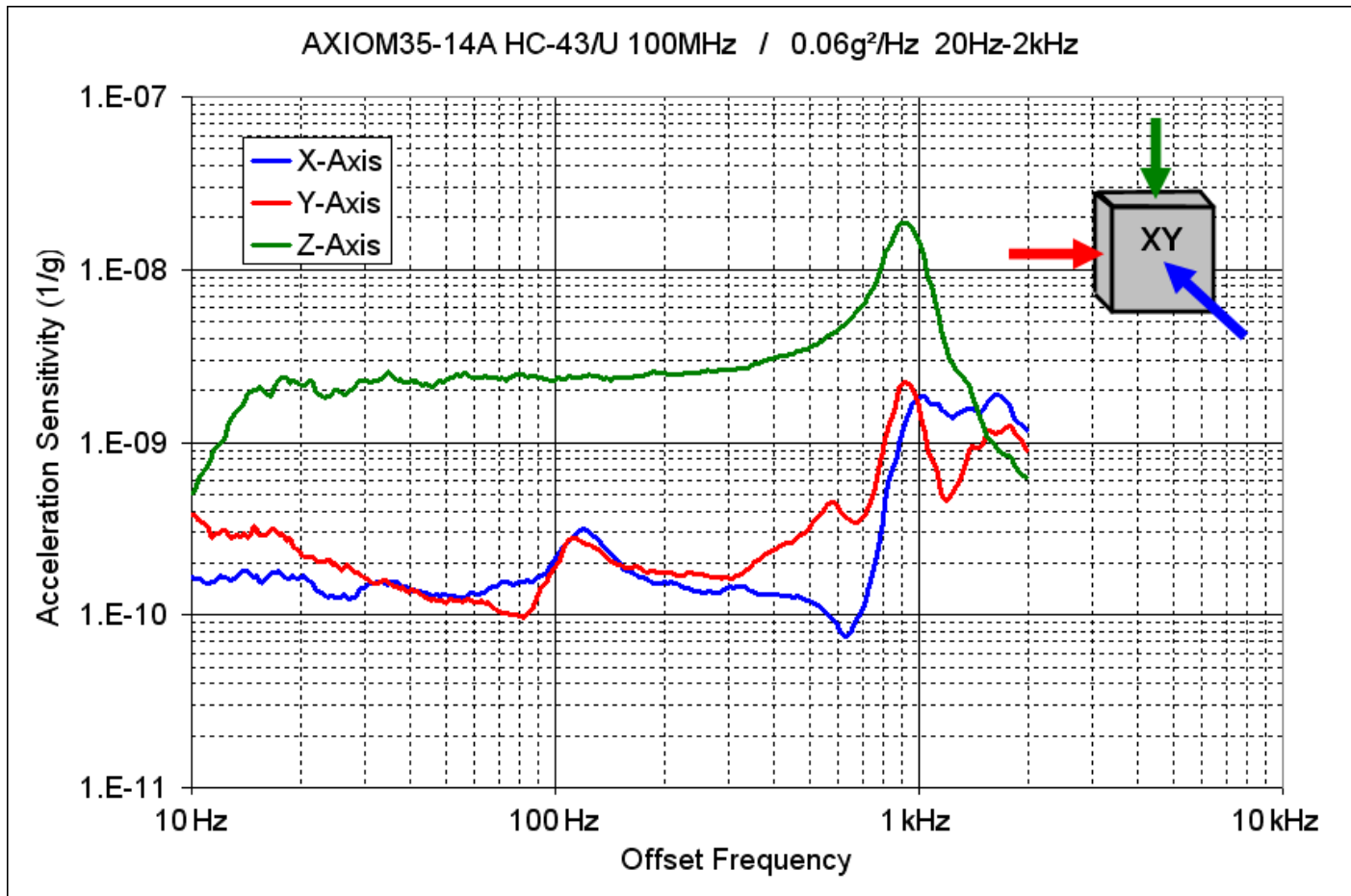
# AXIOM35-14A-100 MHz SC-cut (HC-43/U)

## Phase noise

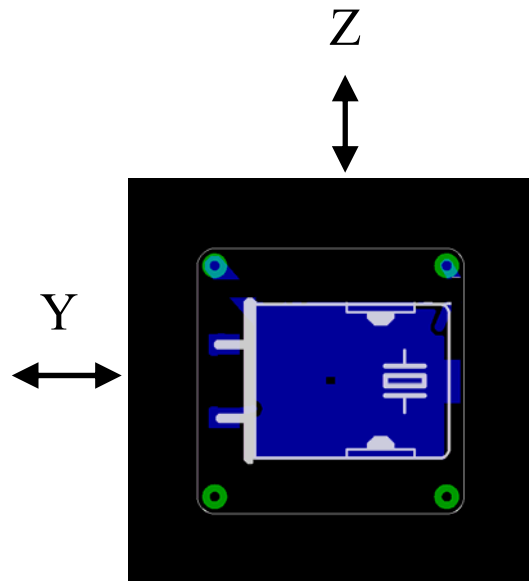


# AXIOM35-14A-100 MHz SC-cut (HC-43/U)

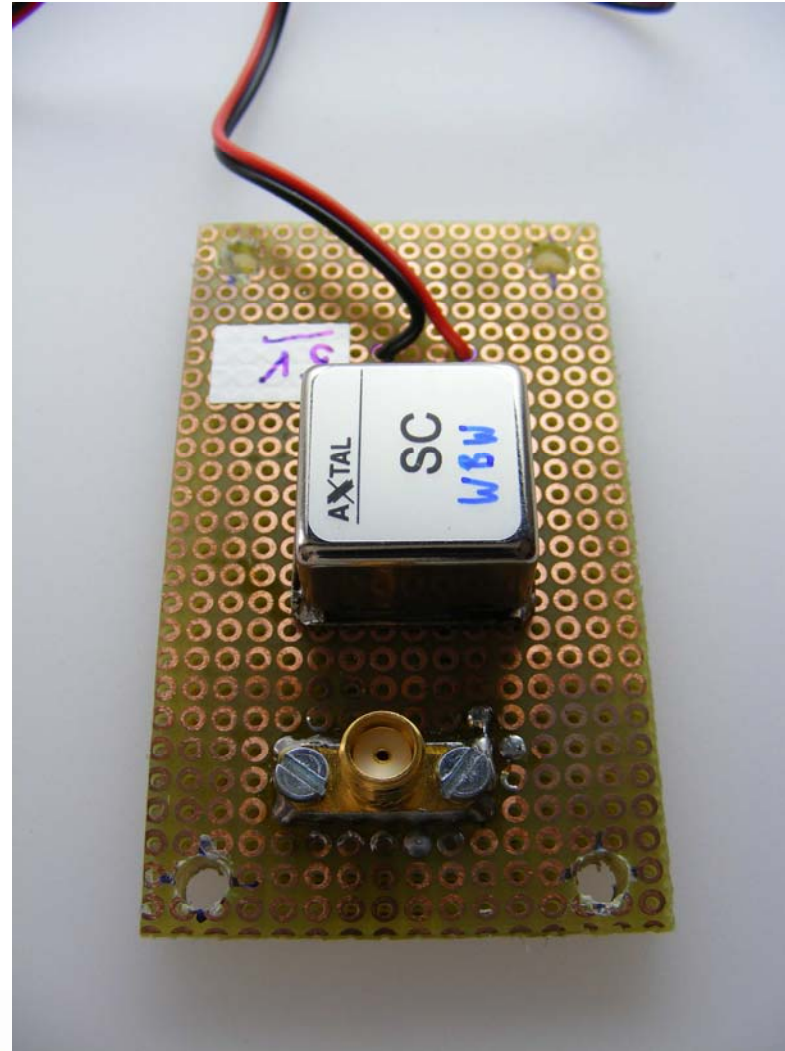
## G-Sensitivity



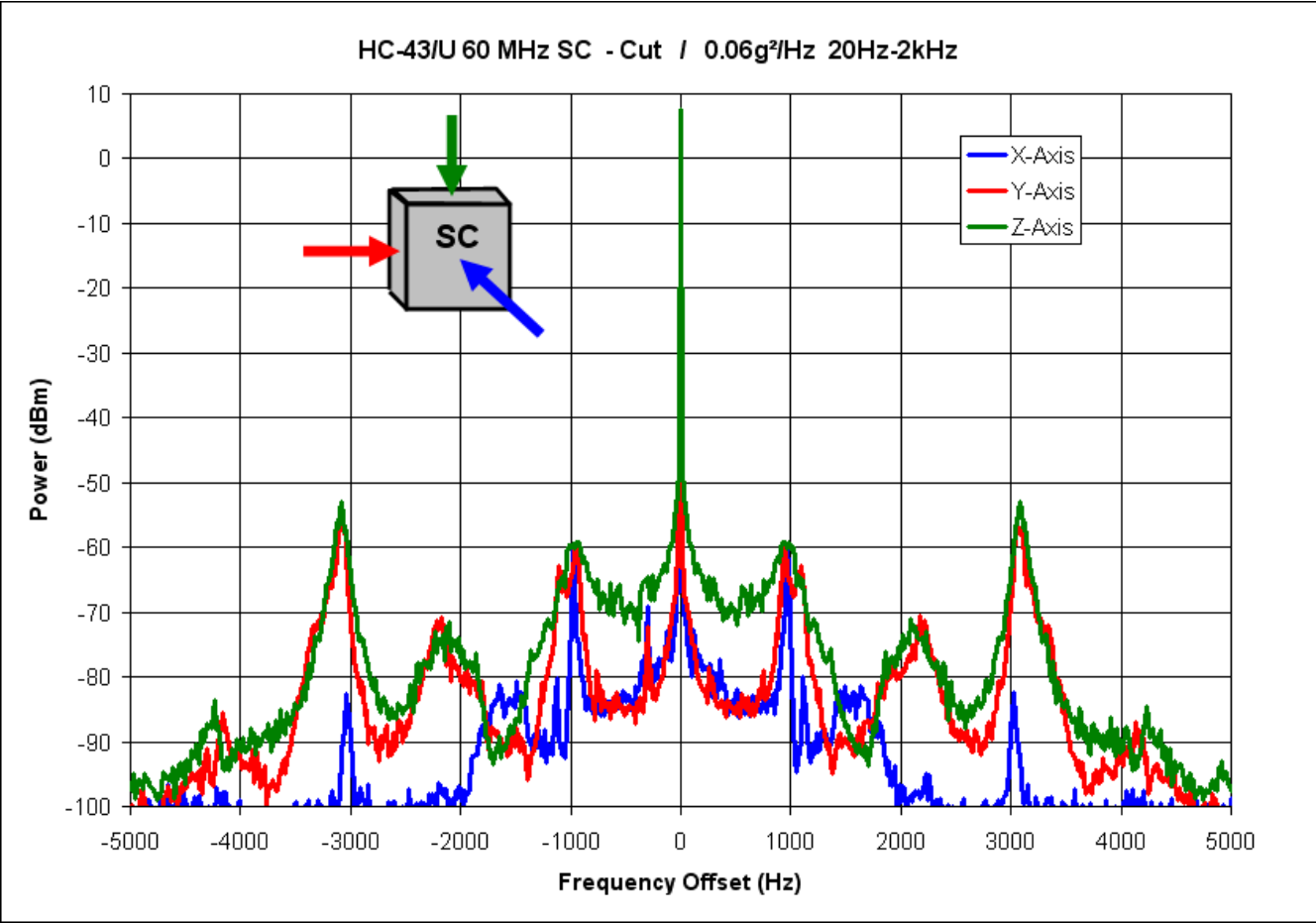
# 60 MHz SC-cut (HC-43/U) other vendor Test fixture



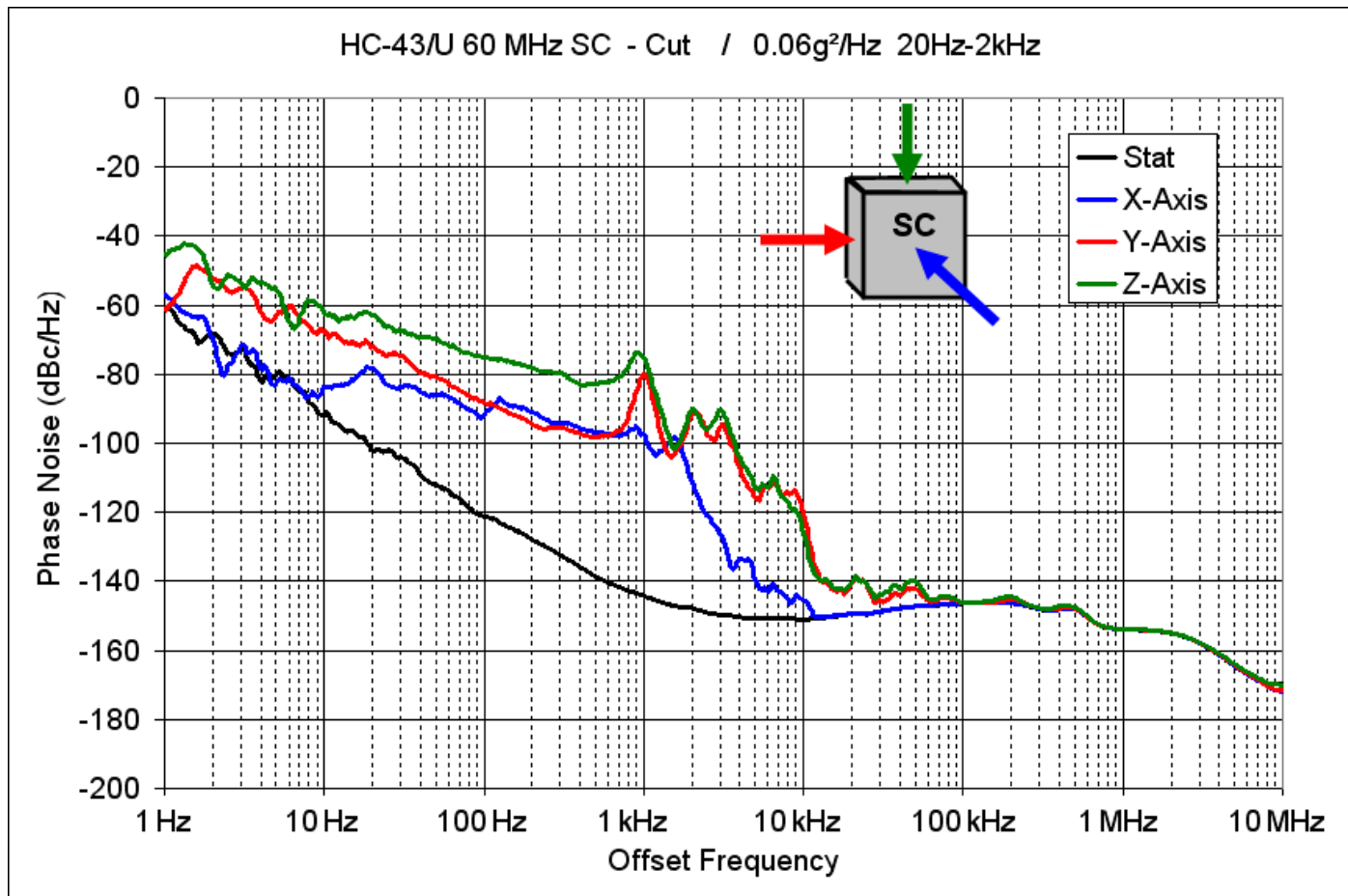
Orientation



# 60 MHz SC-cut (HC-43/U) other vendor Output Spectrum



# 60 MHz SC-cut (HC-43/U) other vendor Phase noise



# 60 MHz SC-cut (HC-43/U) other vendor G-Sensitivity

